

**Exam. # 2 of Physical Chemistry for Energy Science**  
**Department of Nuclear Engineering, Seoul National University**  
**11/21/01 Wednesday PM 2:30-4:30**  
**Two hour, closed book, formula booklet, one spike sheet allowed**

1. (15) For the ammonia production process with the following reaction;  
$$(1/2) \text{N}_2 + (3/2) \text{H}_2 = \text{NH}_3$$
one mole of nitrogen and three moles of hydrogen are inserted into a reaction chamber and completely reacted at one atmosphere.
  - (a) Determine heat of reaction for the above reaction, if reacted isothermally at room temperature
  - (b) Determine adiabatic flame temperature, assuming all specific heat at room temperature apply for the entire range.
  
2. (10) For a pure substance, describe the followings
  - (a) procedure to construct its phase diagram for the first order transition.
  - (b) the second order transition.
  
3. (10) Starting from the condition that chemical potential of phase  $\alpha$  and  $\beta$  are equal for a pure substance, show that;  
$$dP/dT = \Delta H_m^{\alpha\beta} / (T^{\alpha\beta} \Delta V^{\alpha\beta})$$
where  $\Delta H_m^{\alpha\beta}$  is the latent heat for the phase transformation.
  
4. (10) Using  $dA = -SdT - PdV + \gamma dA + \mu dn$ , show that the condition for a liquid drop and its vapor at equilibrium is;  
$$\mu^v = \mu^l + 2\gamma M / \rho r$$
where  $\gamma$ ,  $M$ ,  $\rho$  and  $r$  are surface tension, molar mass, density and the radius of droplet, respectively.
  
5. (15) For an ideal gas,
  - (a) Show that the molar internal energy can be determined from the following relationship:

$U - U_0 = RT^2 \left( \frac{\partial \ln z}{\partial T} \right)$ ,  
 where  $U_0$  is  $U$  at 0 K.

(b) A gas container containing 10 moles of the gas has a pressure of 1 atm. at room temperature. The translational partition function is given for a molecule, as follows;

$$z_{\text{trans}} = (2\pi mk)^{3/2} V/h^3$$

Start =  $\frac{2N}{h^3}$

$\frac{1}{h^3}$

Then, derive a statistical expression for total internal energy

6. (15) Atoms in a single crystal are found to have vibration energy states that are separated by a constant difference,  $\epsilon_0$ .

(a) Show that the partition function of the material is;

$$z = 1/[1 - \exp(-\epsilon_0/kT)]$$

(b) For the material described above, average energy per atom is measured to be  $\epsilon_0$  at a temperature  $T_a$ . Show that;

$$T_a = (\epsilon_0/k) / \ln[1 + (1/a)]$$

7. (10) A real gas has a constant fugacity coefficient of 0.9.

(a) Determine its PVT relationship.

(b) What kind of force can make the above non-ideal behavior?

8. (15) Five moles of CO and ten moles of O<sub>2</sub> gases isothermally reacted to create CO<sub>2</sub> at one atm. and room temperature.

(a) What is the heat of reaction?

(b) What is the extent of reaction.

(b) How will the equilibrium change if temperature is increased?

**END (Two pages, 8 problem sets)**